

# Central Limit Theorem "CLT"

When is a Sampling distribution normal?

## Central Limit Theorem

A sampling distribution for sample means or sample proportions will be normal if the sample size is sufficiently large.

More Data  $\Rightarrow$  Smaller Standard Error  $\Rightarrow$  More Normal

When is a Sampling distribution for Sample means normal?

\* If population is skewed...

Sample size must be at least 30 ( $n \geq 30$ )

\* If population is normal...

Sampling distribution will be normal also (even if  $n < 30$ )

Estimating Population Means: Sample Data should be normal or have a sample size ( $n$ ) at least 30

When is a Sampling distribution for Sample proportions normal?

Must have at least 10 successes ( $X \geq 10$ ) AND at least 10 failures ( $n - X \geq 10$ )

Example: Graduation?

\* Sample data should have at least 10 graduates and at least 10 that did not graduate.

\* What sample size should we use?

Suppose population grad. rate = 0.275

Use Larger of these two

$$n = \frac{10}{\pi}$$

$$\text{or } n = \frac{10}{1 - \pi}$$

We need sample size at least 37

Why does Sampling Distribution need to be normal?

Accuracy of formulas using the mean and Standard Error  
Critical T and Z-scores

(For Sample size, Round up)

$$n = \frac{10}{\pi} = \frac{10}{0.275} = 36.3636 \approx 37$$

$$n = \frac{10}{(1 - \pi)} = \frac{10}{(1 - 0.275)} = 13.7931$$